




JaxNRSur - Numerical Relativity Surrogates in JAX

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Summary

The detection and analysis of gravitational waves rely on accurate and efficient modeling of waveforms from compact binary coalescences. Numerical relativity (NR) surrogate models are a family of data-driven models that are directly trained on NR simulations to provide fast and accurate approximations of these waveforms without many assumptions about the form of the model.

JaxNRSur is a Python library that implements NR waveform models in JAX ([Bradbury et al., 2018](#)), a high-performance numerical computing library that supports automatic differentiation, just-in-time (JIT) compilation, and hardware acceleration (GPU/TPU). By using JAX, JaxNRSur provides the following key features:

Key features

- **Accelerator support:** The same code runs efficiently on CPUs, GPUs, and TPUs, with no user intervention required. This allows for fast waveform evaluations in large-scale analyses.
- **Simple vectorization:** JAX's vectorization capabilities allow users to efficiently evaluate waveforms for multiple source parameters or times in parallel.
- **Automatic differentiation:** Compute gradients of waveforms with respect to time, source parameters, or model parameters (i.e., the data in the surrogate model) automatically, enabling advanced inference techniques such as gradient-based sampling or optimization.
- **Unified interface:** A consistent and user-friendly interface for accessing different NR surrogate models, making it easy to switch between models.

JaxNRSur currently includes implementations of several NR surrogate models, including:

- **NRHybSur3dq8:** A hybridized surrogate model for non-precessing binary black hole mergers ([Varma, Field, Scheel, Blackman, Kidder, et al., 2019](#)), valid for mass ratios up to 8.
- **NRSur7dq4:** A surrogate model for precessing binary black hole mergers ([Varma, Field, Scheel, Blackman, Gerosa, et al., 2019](#)), valid for mass ratios up to 4.

We have validated our implementation against the original implementations of these models in gwsurrogate ([Field et al., 2025](#)) to ensure correctness and consistency. The package also includes utilities for downloading and caching the required data files from Zenodo ([European Organization For Nuclear Research & OpenAIRE, 2013](#)), making it easy to set up and use.

Statement of need

The original implementations of NR surrogate models in `gwsurrogate` (Field et al., 2025) are mainly implemented in `numpy` and `scipy` with additional bindings from `c`, which gives the package reasonable performance. However, this implementation does not take advantage of more modern computing paradigms such as the use of accelerators (GPUs/TPUs) and automatic differentiation, which have been widely adopted in the machine learning and high-performance computing communities. This presents a few challenges when using and developing NR surrogate models, and this package aims to address these challenges:

A main challenge in using NR surrogate models for downstream tasks such as parameter estimation is the relatively high computational cost compared to other waveform approximants such as `IMRPhenomXPHM` (Pratten & others, 2021). NR surrogate models involve a lot of dense matrix multiplications and other linear algebra operations, which can be efficiently parallelized on accelerators such as GPUs and TPUs. This JAX implementation allows users to leverage accelerators to speed up waveform evaluations. For example, in a publicly available benchmark on an NVIDIA T4 GPU in a Google Colab environment, the `NRSur7dq4` waveform can be evaluated for 100 parameters in approximately 65 ms, which is significantly faster than the original implementation in `gwsurrogate`¹. This speedup is further compounded by the fact that JAX supports vectorization of functions that is accelerator-aware, providing the performance the NR surrogate model family needs for downstream tasks.

Another feature this package provides is the ability to compute gradients of the waveform with respect to the source parameters through automatic differentiation. This is useful for tasks such as template bank generation (Coogan et al., 2022) or gradient-based Markov chain Monte Carlo (MCMC) sampling (Betancourt, 2017) (Wong et al., 2023) (Cabezas et al., 2024). Parallel to the improvement in waveform evaluation throughput, being able to leverage gradient information often speeds up the convergence of these downstream tasks, which further improves the performance of a complete pipeline when compared to non-gradient-based counterparts. On top of performance gains, higher-order derivatives such as Hessians can be used as a natural metric for understanding uncertainties in the pipeline and help in sensitivity analysis.

Finally, this package also supports differentiating with respect to the model parameters in a fashion similar to how neural networks are trained. This allows users to fine-tune the model parameters to better fit their data (Lam et al., 2024). Another research avenue our package opens is more flexible ways to incorporate uncertainties into the models. Similar to how neural networks can be promoted to probabilistic models through techniques such as Bayesian neural networks (Jospin et al., 2020), the gradient information allows users to more efficiently fit a large number of model parameters, enabling the possibility of promoting each model parameter to a distribution rather than a point estimate. This can be useful for understanding systematics and uncertainties in the models, which is crucial for accurate gravitational wave analyses.

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¹Benchmarking results on Google Colab may vary depending on the specific hardware and software environment that is provisioned.

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